

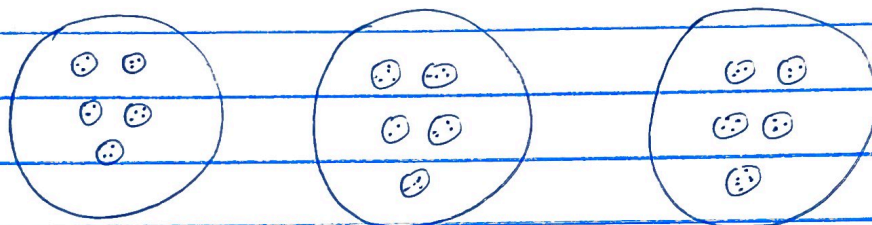
Section 3-4 Multiplication of Whole #s

Models for Whole Number Multiplication

1. Repeated Addition

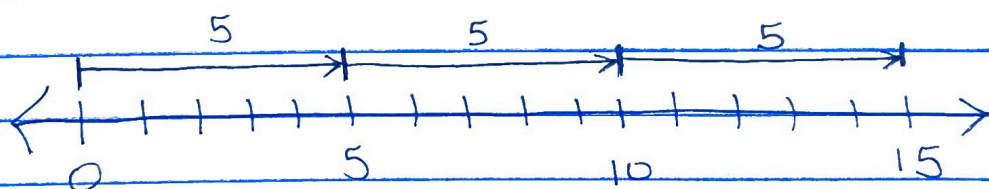
$$3 \times 5 = 5 + 5 + 5 = 15$$

Sets:

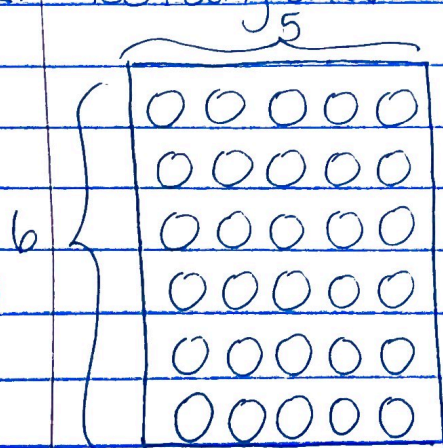


union of these sets is 15

Number
Line

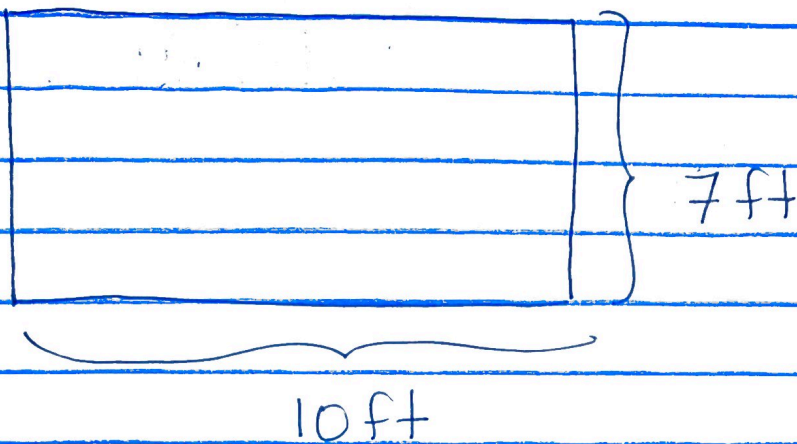


2. Rectangular Array / Area Model



How many mini muffins are
in the pan?

$$6 \times 5 = 30$$

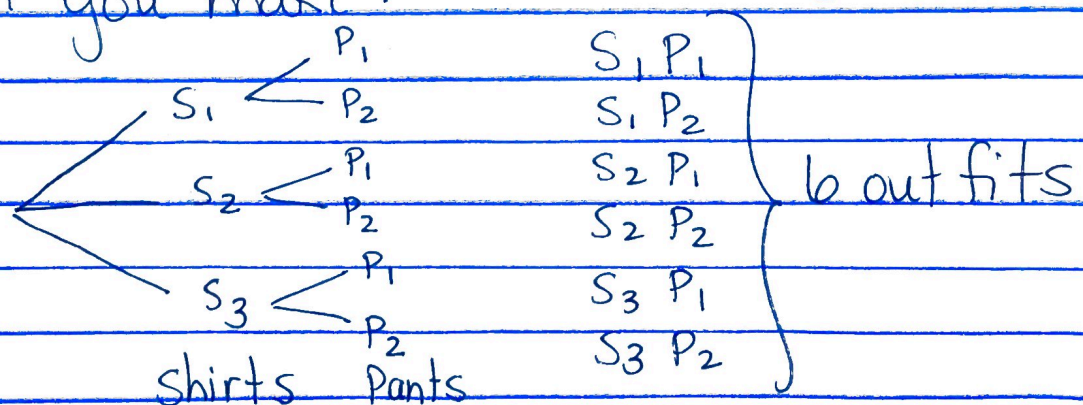


How many 1 ft by 1 ft tiles are needed to cover a floor that is 10 ft by 7 ft?

$$10 \times 7 = 70 \text{ sq. feet}$$

3. Cartesian Product

On a trip, you pack 3 shirts and 2 pairs of pants. How many outfits can you make?



Properties of Whole # Multiplication

1. Closure Property

The product of any 2 whole #s is always a whole number.

2. Commutative Property

$$\text{ex: } 6 \cdot 5 = 5 \cdot 6$$

3. Associative Property

$$\text{ex: } 3(2 \cdot 5) = (3 \cdot 2) \cdot 5$$

4. Identity Property

$$\text{ex: } 7 \cdot 1 = 1 \cdot 7 = 7$$

5. Zero Multiplication Property

$$\text{ex: } 6 \cdot 0 = 0 \cdot 6 = 0$$

6. Distributive Property of Mult over Add/Sub

$$\text{ex: } 5(3+6) = 5 \cdot 3 + 5 \cdot 6$$

$$\text{ex: } 4(10-2) = 4 \cdot 10 - 4 \cdot 2$$

Algorithms For Whole # Multiplication

1. Standard Algorithm

$$\begin{array}{r} 36 \\ \times 14 \\ \hline 144 \\ + 360 \\ \hline 504 \end{array}$$

Why do we put a 0 here? bc we move to the tens place value to multiply

2. Partial Products

Vertical:

$$\begin{array}{r} 36 \\ \times 14 \\ \hline 24 \leftarrow 6 \times 4 \\ 120 \leftarrow 4 \times 30 \\ 60 \leftarrow 6 \times 10 \\ + 300 \leftarrow 30 \times 10 \\ \hline 504 \end{array}$$

Horizontal:
(uses dist prop)

$$\begin{aligned} 36 \times 14 &= (30 + 6)(10 + 4) \\ &= 30 \times 10 + 30 \times 4 + 6 \times 10 + 6 \times 4 \\ &= 300 + 120 + 60 + 24 \\ &= 504 \end{aligned}$$

3. Multiplication by Powers of 10

Multiplying by 10^n increases the place value by n places.

For ex: $5 \cdot 10^2 = 5 \cdot 100 = 500$

Since place values are powers of 10, multiplying by powers of 10 simply increase place value.

Pointing out that:

$$5 \times 100 = 500$$

$$3 \times 100 = 300$$

$$7 \times 10 = 70$$

$$7 \times 1000 = 7000$$

$$12 \times 100 = 1200$$

$$23 \times 10 = 230$$

$$\underline{6} \times \underline{30} = \underline{180}$$

$$\underline{7} \times \underline{200} = \underline{1400}$$

is helpful when starting multiplication with multidigit numbers.

36×14 using partial products / Area

	30	+	6
10	$30 \times 10 = 300$		$6 \times 10 = 60$
+			
4	$30 \times 4 = 120$		$6 \times 4 = 24$

$$\begin{array}{r} 300 \\ 120 \\ 60 \\ + 24 \\ \hline 504 \end{array}$$

This is a good technique to start multiplying multidigit numbers bc it breaks the problem into manageable pieces. The kids don't have to remember order or where to put certain things.

52×7

	50	+	2
7	$50 \times 7 = 350$		$7 \times 2 = 14$

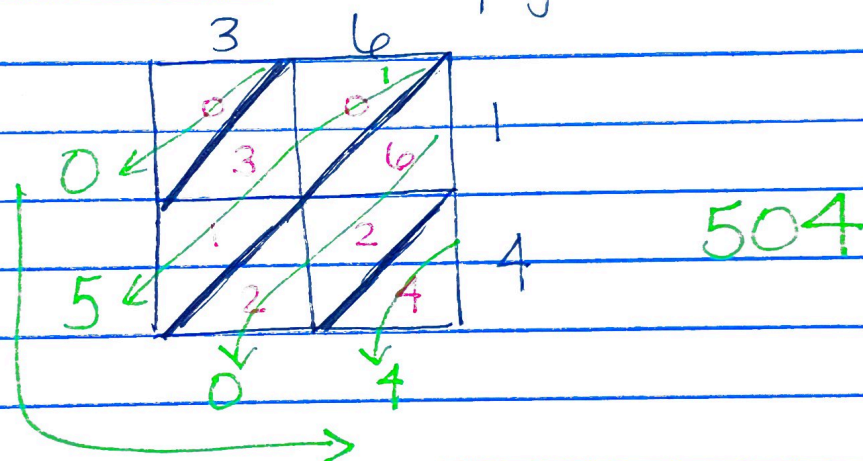
$$\begin{array}{r} 350 \\ + 14 \\ \hline 364 \end{array}$$

4. Lattice Multiplication

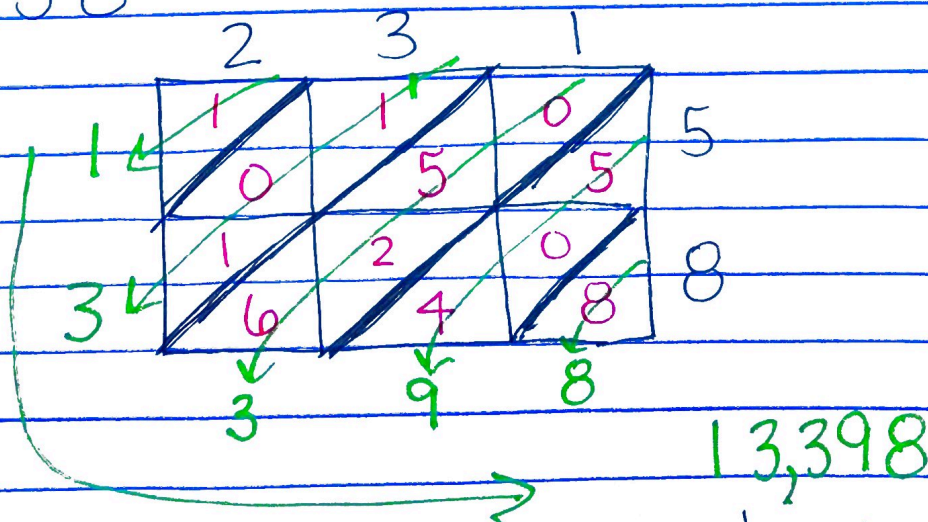
People mistakenly call this "new math" when, in fact, this technique has been around since the 10th century. It is becoming more utilized due to its structural approach to multiplication.

ex 1 Use lattice to multiply.

a) 36×14



b) 231×58



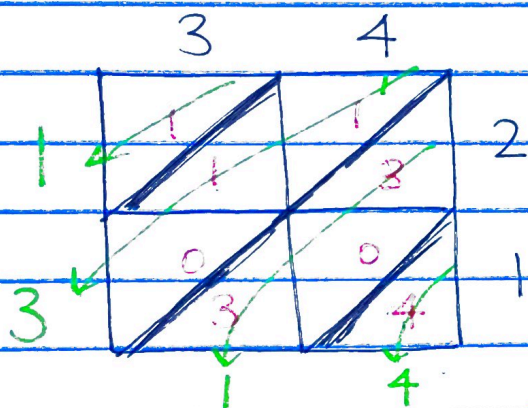
end 3-4 part 1

Multiplication in Other Bases

Lattice multiplication is extremely useful when multiplying in other bases.

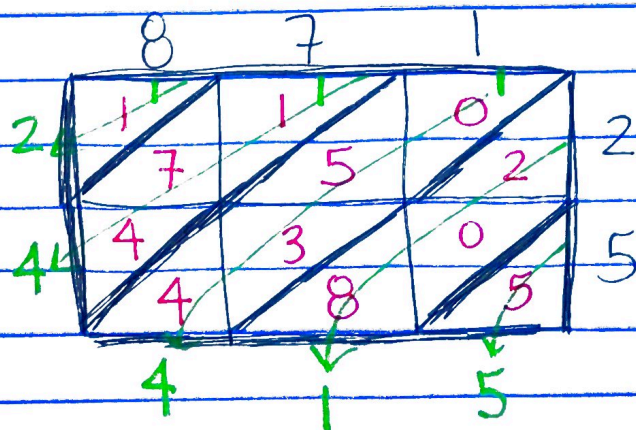
ex 2 Multiply

a) $34_{\text{five}} \times 21_{\text{five}}$



1314_{five}

b) $871_{\text{nine}} \times 25_{\text{nine}}$



24415_{nine}

$7 \times 2 = 14$

1 grp of 9 + 5 ones

$7 \times 5 = 35$

3 grps of 9 + 8 ones

$8 \times 5 = 40$

4 grps of 9 + 4 ones

Mental Multiplication Techniques

1. Front End Multiplication

ex 3 Multiply Mentally

$$\begin{aligned} \text{a) } 36 \times 8 &\Rightarrow (30 + 6) \times 8 = (30 \times 8) + (6 \times 8) \\ &= (240) + (48) \\ &= 288 \end{aligned}$$

$$\begin{aligned} \text{b) } 52 \times 3 &\Rightarrow (50 + 2) \times 3 = 50 \times 3 + 2 \times 3 \\ &= 150 + 6 \\ &= 156 \end{aligned}$$

2. Compensation

ex 4 Multiply

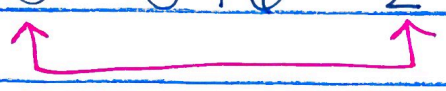
$$\begin{aligned} \text{a) } 12 \times 9 &= 12 \times (10 - 1) \\ &= 12 \times 10 - 12 \times 1 \\ &= 120 - 12 \\ &= 108 \end{aligned}$$

$$\begin{aligned} \text{b) } 45 \times 98 &= 45 \times (100 - 2) \\ &= (45 \times 100) - (45 \times 2) \\ &= 4500 - 90 \\ &= 4410 \end{aligned}$$

3. Compatible Numbers

ex 5 Multiply

a) $5 \times 346 \times 2 = 346 \times 10 = 3460$



b) $25 \times 9 \times 11 \times 4 = 100 \times 99 = 9900$



c) $2 \times 9 \times 5 \times 20 \times 5 = 10 \times 100 \times 9 = 9000$



All of these mental techniques are geared toward multiplying bigger numbers.

What about mental techniques for learning basic multiplication facts?

	Mult by 2 $\Rightarrow$ Double	
	Mult by 3 $\Rightarrow$ Double then add 1 group	
Core	Mult by 5 $\Rightarrow$ skip count by 5	
	Mult by 9 $\Rightarrow$ finger trick or digit pattern	
	Mult by 10 $\Rightarrow$ add a zero	$9 \times 1 = 9$
	Mult by 4 $\Rightarrow$ Double 2	$9 \times 2 = 18$
	Mult by 6 $\Rightarrow$ Double 3	$9 \times 3 = 27$
Build off of core	Mult by 7 $\Rightarrow$ 5 and 2	$9 \times 4 = 36$
	Mult by 8 $\Rightarrow$ 5 and 3	$9 \times 5 = 45$
	Mult by 11 $\Rightarrow$ 10 and 1	$9 \times 6 = 54$
	Mult by 12 $\Rightarrow$ 10 and 2	$9 \times 7 = 63$
		$9 \times 8 = 72$
		$9 \times 9 = 81$

$$\begin{aligned}
 \text{So, } 9 \times 12 &= 9 \times 10 + 9 \times 2 \\
 &= 90 + 18 \\
 &= 108
 \end{aligned}$$

Estimating Whole # Mult + Division

The only useful technique for estimating whole # multiplication is rounding.
and division

End 3-4