

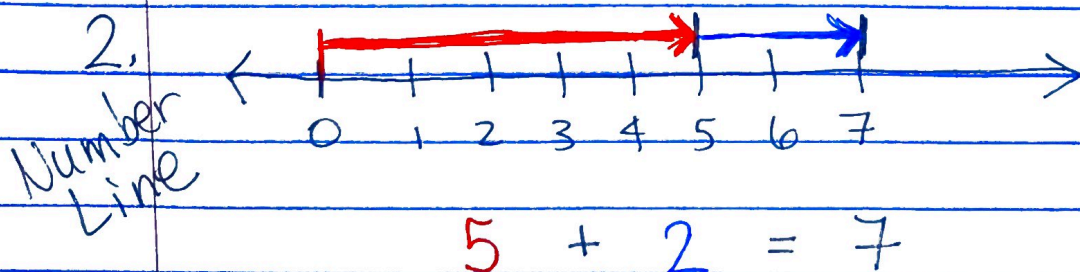
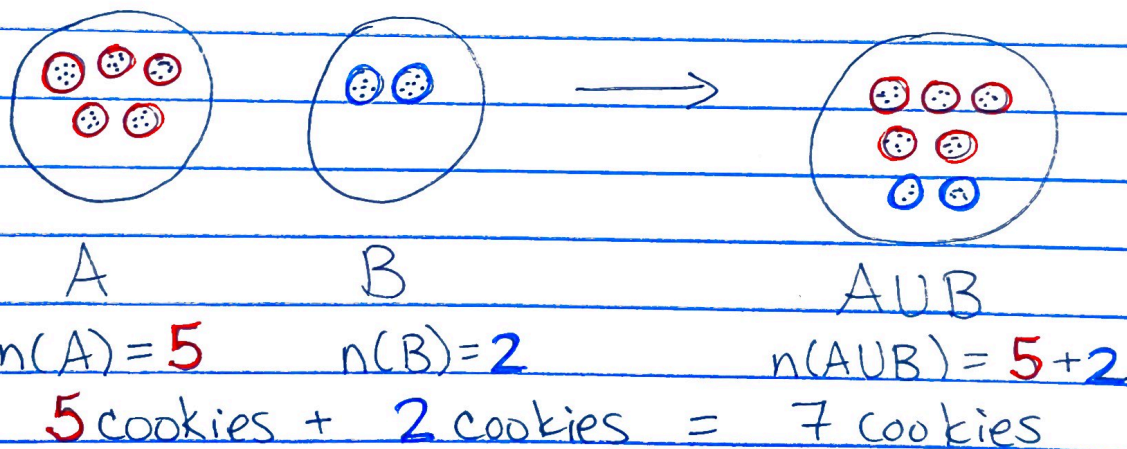
Section 3-2 Addition of Whole #s

Whole #s $\{0, 1, 2, 3, 4, 5, \dots\}$

Natural #s $\{1, 2, 3, 4, \dots\}$
(Counting Numbers)

Models for Whole # Addition

1. Set Model: If A and B are 2 disjoint, finite sets and $n(A) = a$ and $n(B) = b$ then $a + b = n(A \cup B)$.



* The number line is helpful for organizing and comparing whole numbers. The farther to the right, the greater the value.

Properties of Whole Number Addition

1. closure

The sum of any 2 whole numbers is always a whole number.

2. commutative

(commute = exchange)

ex: $3 + 2 = 2 + 3$

3. associative

ex: $3 + (7 + 5) = (3 + 7) + 5$

4. Identity property of addition

ex: $5 + 0 = 5$ and $0 + 5 = 5$

* 0 is called the additive identity element
Identity = Identical = Same.

ex 1 Which property is illustrated?

a) $(\underline{3 + 2}) + 8 = (\underline{2 + 3}) + 8$ commutative

b) $5 + 10$ is a unique whole number closure

c) $(6 + 3) + 1 = 6 + (3 + 1)$ associative

Mastering Basic Addition Facts

There are several strategies to help kids master basic addition facts.

1. Counting On (Counting Up)

You start at one addend and count up the other addend.

ex: $4 + 2 \rightarrow 4, 5, 6$

Start $\xrightarrow{\text{count up 2 more}}$

$4 + 2 = 6$
$\swarrow \quad \searrow$
addends sum

* In Kindergarten, my son could find $7 + 3$ easily, but struggled with $3 + 7$. Why do you think this happened?
He didn't understand the commutative property.

2. Doubles Benchmark

If a child can master the addition in pairs ($3 + 3$, $6 + 6$, $7 + 7$, ...) then this knowledge can be extended to doubles + 1, doubles + 2, ...

ex: $6 + 7 = (6 + 6) + 1$

$6 + 8 = (6 + 6) + 2$

3. Making Ten (Compatible Numbers)

You can split up one of the addends in order to "make ten" then add in the leftovers. (This extends to any multiple of 10.)

$$\text{ex: } 8 + 5 = 8 + (2 + 3) = (8 + 2) + 3$$

$$\text{ex: } 13 + 9 = (13 + 7) + 2 = 20 + 2$$

Whole Number Addition Algorithms

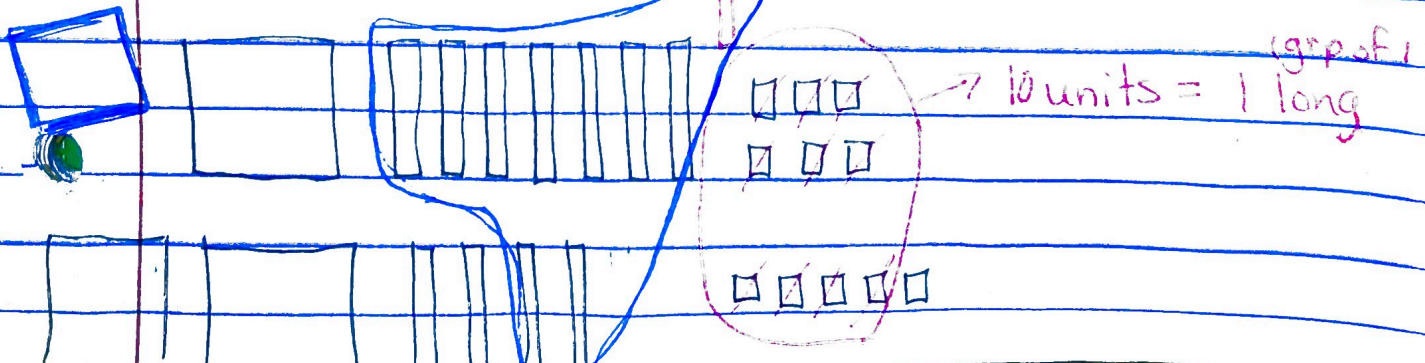
1. Standard Algorithm

$$\begin{array}{r} 176 \\ + 245 \\ \hline 421 \end{array}$$

represents 1 group of 100

represents 1 group of 10

2. Base 10 Blocks



3. Partial Sums

$$\begin{array}{r}
 176 \\
 + 245 \\
 \hline
 111 \leftarrow 6+5 \\
 + 110 \leftarrow 70+40 \\
 \hline
 300 \leftarrow 100+200 \\
 + 421 \\
 \hline
 421
 \end{array}$$

* This technique emphasizes place value.

4. Lattice Addition

$$\begin{array}{r}
 176 \\
 + 245 \\
 \hline
 \begin{array}{|c|c|c|}
 \hline
 0 & 3 & 1 \\
 \hline
 \end{array} \\
 \begin{array}{c}
 \swarrow \\
 \downarrow \\
 \searrow
 \end{array}
 \end{array}$$

This is a compressed version of partial sums.

5. Left to Right Addition

$$\begin{array}{r}
 176 \\
 + 245 \\
 \hline
 300 \leftarrow 100+200 \\
 + 110 \leftarrow 70+40 \\
 \hline
 11 \leftarrow 6+5 \\
 \hline
 421
 \end{array}$$

$$\begin{array}{r}
 176 \\
 + 245 \\
 \hline
 \cancel{3} \cancel{0} \cancel{0} \\
 421
 \end{array}$$

* Kids read left to right, so it makes sense that they would try to do math left to right.

* I've noticed that when kids use base 10 blocks, they tend to combine the largest ones first.

6. Scratch Addition

This algorithm is useful when adding a bunch of numbers. Each "scratch" represents 10.

$$\begin{array}{r} 33 \\ 46 \\ 27 \\ 13 \\ 04 \\ 59 \\ + 382 \\ \hline 308 \end{array}$$

Diagram illustrating Scratch Addition. A vertical pink line separates the numbers into two columns. The numbers are stacked vertically: 33, 46, 27, 13, 04, 59, and 382. A plus sign is to the left of 382. The numbers 27, 13, 04, and 382 have their tens digits crossed out with a red slash. The final sum, 308, is written in pink at the bottom. A red arrow points from the crossed-out 2 in 27 down to the 0 in 308.

end 3-2
part 1

Adding in Bases Other than 10

ex 2 Add

a)

$$\begin{array}{r} \\ 4 \ 2 \ 3 \text{ five} \\ + \quad 3 \ 4 \text{ five} \\ \hline 1 \ 0 \ 1 \ 2 \text{ five} \end{array}$$

b)

$$\begin{array}{r} \\ 8 \ 6 \ 4 \text{ twelve} \\ + \text{I} \ 9 \ 7 \text{ twelve} \\ \hline 1 \ 7 \ 3 \ \text{E} \text{ twelve} \end{array}$$

c)

$$\begin{array}{r} \\ 2 \ 3 \ 1 \text{ four} \\ \cancel{2} \cancel{3} \text{ four} \\ \cancel{1} \cancel{3} \text{ four} \\ \cancel{2} \cancel{2} \text{ four} \\ \cancel{2} \text{ four} \\ \text{ four} \\ + \text{ four} \\ \hline 2 \ 2 \ 1 \text{ four} \end{array}$$

scratch method
each scratch
represents a
group of 4

Mental Addition Techniques

1. Compatible Numbers

ex 3 Add

a) $120 + 94 + 36 = 120 + 130 = \boxed{250}$

b) $120 + 50 + 35 + 80 + 50 = 200 + 100 + 35 = \boxed{335}$

c) $45 + 71 + 16 + 10 + 9 + 45 = 100 + 80 + 16 = \boxed{196}$

2. Adding From the Left

ex 4 Add

a) $58 + 25 \Rightarrow \begin{array}{l} 50 + 20 = 70 \\ 8 + 5 = 13 \end{array} \left. \vphantom{\begin{array}{l} 50 + 20 = 70 \\ 8 + 5 = 13 \end{array}} \right\} \begin{array}{r} 70 \\ + 13 \\ \hline 83 \end{array}$

b) $72 + 49 \Rightarrow \begin{array}{l} 70 + 40 = 110 \\ 2 + 9 = 11 \end{array} \left. \vphantom{\begin{array}{l} 70 + 40 = 110 \\ 2 + 9 = 11 \end{array}} \right\} \begin{array}{r} 110 \\ + 11 \\ \hline 121 \end{array}$

3. Substitution (Breaking up + Bridging)

ex 5 Add

$$\begin{aligned} \text{a) } 127 + 38 &= (127 + 3) + 35 \\ &= 130 + 35 = 165 \end{aligned}$$

$$\begin{aligned} \text{b) } 84 + 47 &= (84 + 6) + 41 \\ &= 90 + 41 = 131 \end{aligned}$$

OR

$$\begin{aligned} &= (84 + 16) + 31 \\ &= 100 + 31 = 131 \end{aligned}$$

4. Trading off (Compensation)

ex 6 Add

$$\begin{array}{rcl} 65 & \Rightarrow & 65 + 5 \Rightarrow 70 \\ + 38 & + & 38 - 5 + 33 \\ \hline & & 103 \end{array}$$

* This is very similar to breaking up + bridging.

Estimating whole # Addition

There are 3 ways to estimate addition.

1. Front end estimation

ex:

$$\begin{array}{r} 236 \\ + 141 \\ \hline 680 \end{array}$$

$$200 + 100 + 600 = \boxed{900}$$

2. Grouping to nice numbers

ex:

$$\begin{array}{r} 47 \\ \rightarrow 28 \\ \rightarrow 13 \\ 52 \\ + \rightarrow 9 \\ \hline \end{array}$$

about 50

about 100

The sum is about 150.

3. Rounding

ex: $47 + 28 + 13 + 52 + 9$

Rounds to: $50 + 30 + 10 + 50 + 10 = 150$

end 3-2